

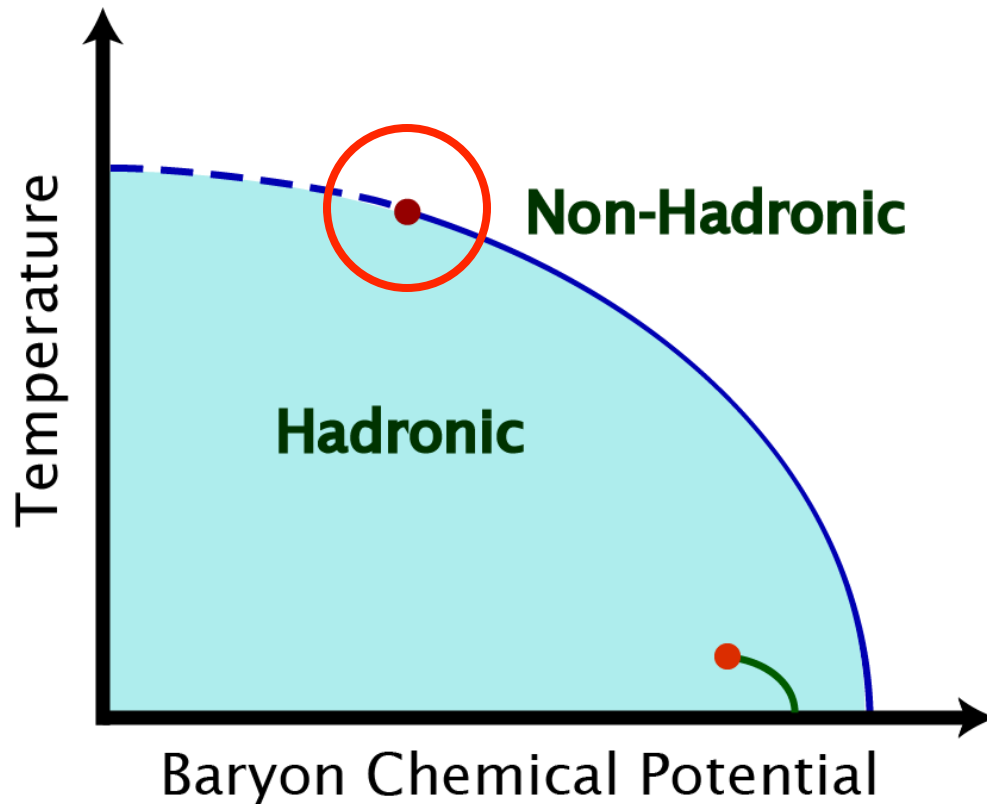


# Energy Dependence of High-Moments of Net-proton Distributions at RHIC

**H.G. Ritter**

**LBL**

For the STAR Collaboration



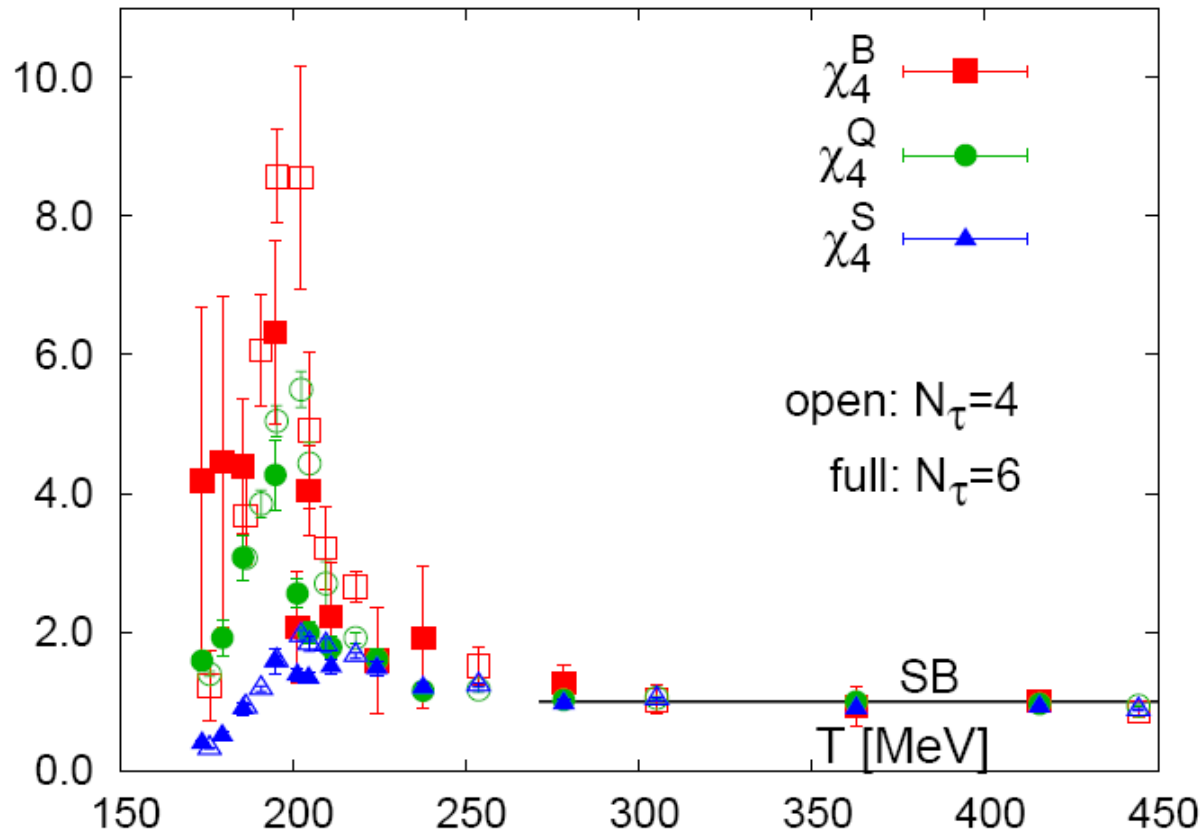
**Critical Point:**  
**Solid State Phys**

- Susceptibilities diverge
- Correlation Length diverges

**Heavy Ions**

- Becomes Critical Region
- Correlation Length  $\xi =$  System size

$\langle (dN)^2 \rangle \sim \xi^2$



Fluctuations of conserved quantities indicate nearby singularities

M. Cheng, et al., arXiv:0811.1006

ICPAQGP 2010, Goa, December 5 - 10

Baryon number susceptibility:

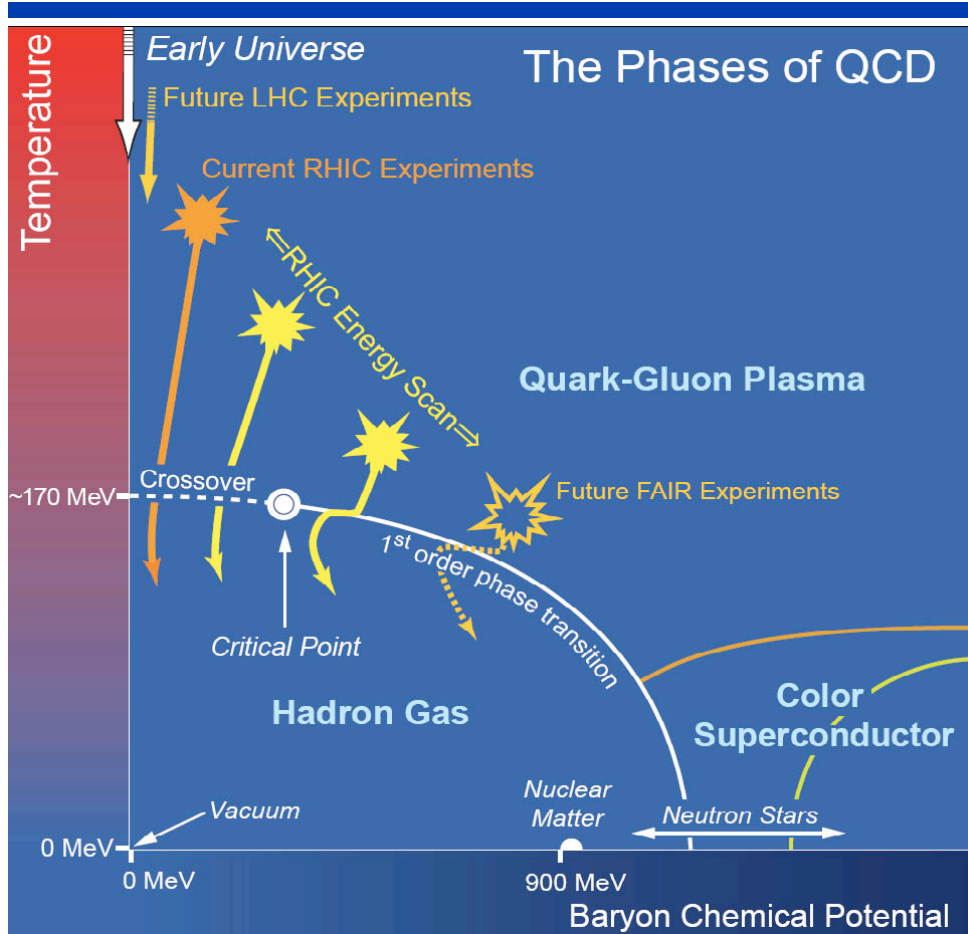
$$\chi_B \sim \langle (\delta B)^2 \rangle$$

Similar for other conserved quantities,  
e.g. charge

→ Connection between lattice and  
fluctuations of conserved quantities  
**Lattice QCD (LQCD) predictions**

→ Critical fluctuations are Non-gaussian

- Non-gaussian fluctuations
- Higher moments sensitive to non-gaussian behavior
  - Kurtosis
  - Skewness
- Higher moments amplify signal



Look for non-monotonic variations of higher moments of conserved quantity distributions as a function of beam energy

Challenging measurement

Caveats:

Critical slowing down  
Dynamical effects

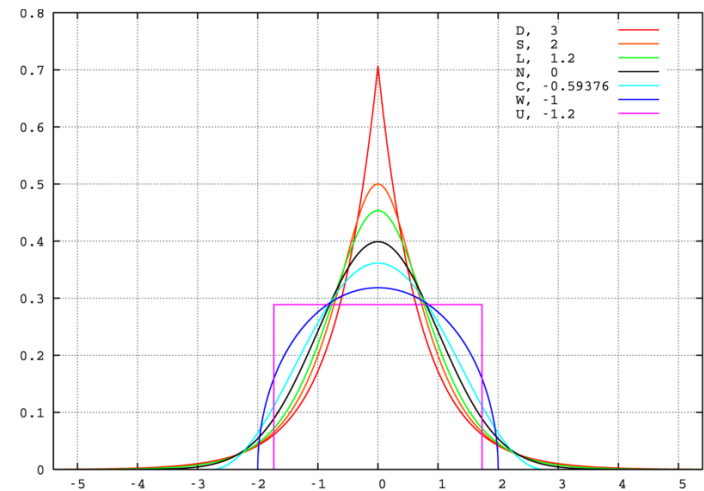
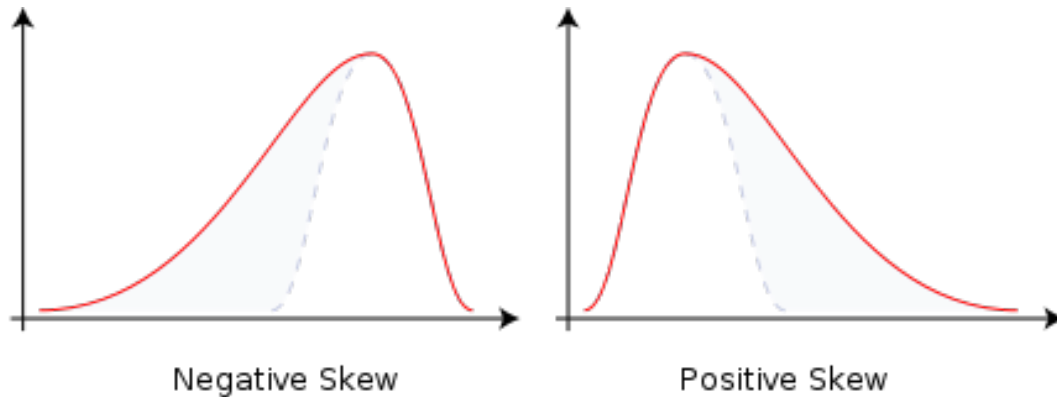
B. Berdnikov & K. Rajagopal, Phys. Rev. D 61, 105017 (2000)  
Stephanov, Rajagopal, Shuryak, Phys. Rev. D 60, 114028 (1999)

**Mean:**  $Y = \langle N \rangle$

**St. Deviation:**  $\sigma = \sqrt{\langle (N - \langle N \rangle)^2 \rangle}$

**Skewness:**  $s = \frac{\langle (N - \langle N \rangle)^3 \rangle}{\sigma^3}$

**Kurtosis:**  $\kappa = \frac{\langle (N - \langle N \rangle)^4 \rangle}{\sigma^4} - 3$



- Skewness describes the **asymmetry** of the distribution
- Kurtosis describes the **peakness** of the distribution
- Equal to zero for Gaussian distribution
- **Ideal probes for non-Gaussian fluctuations**



# Central Limit Theorem

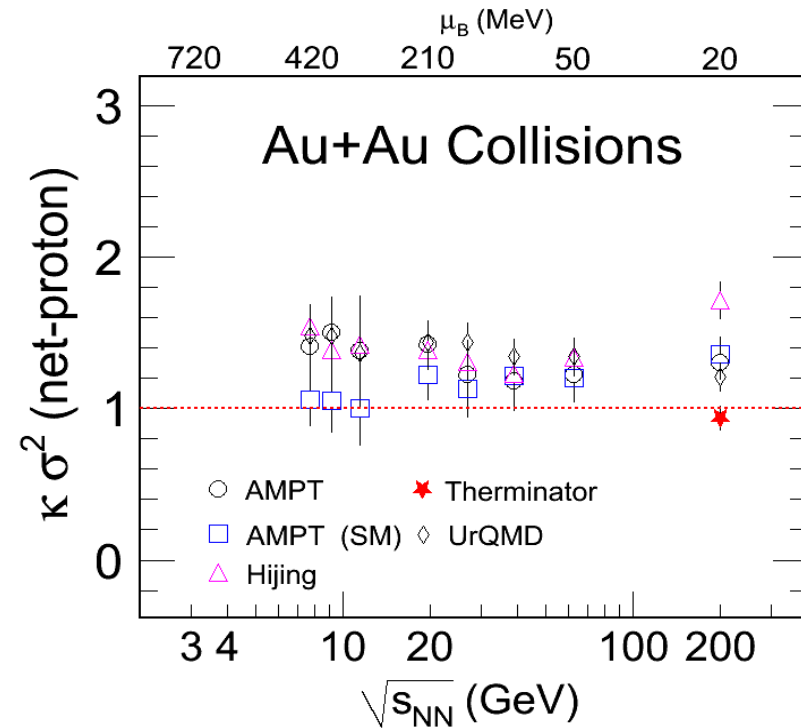
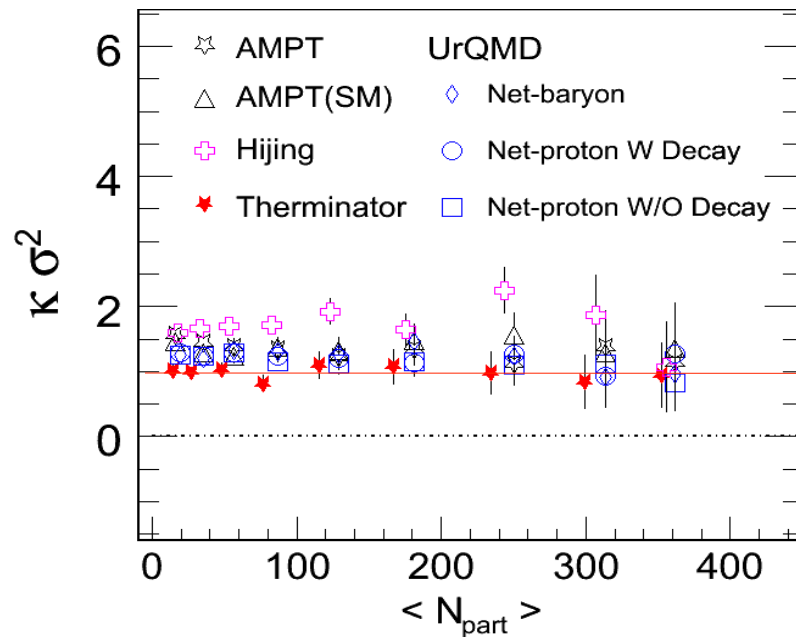


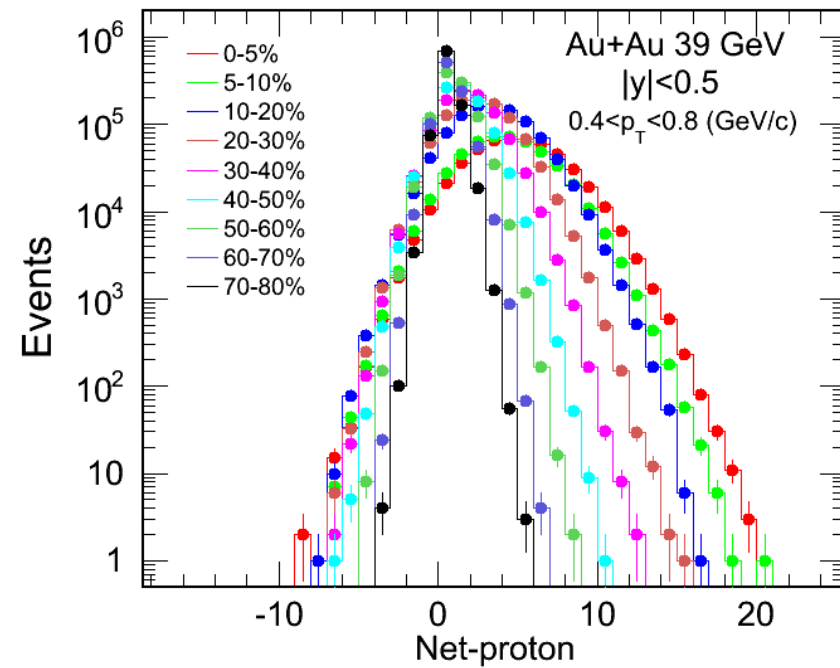
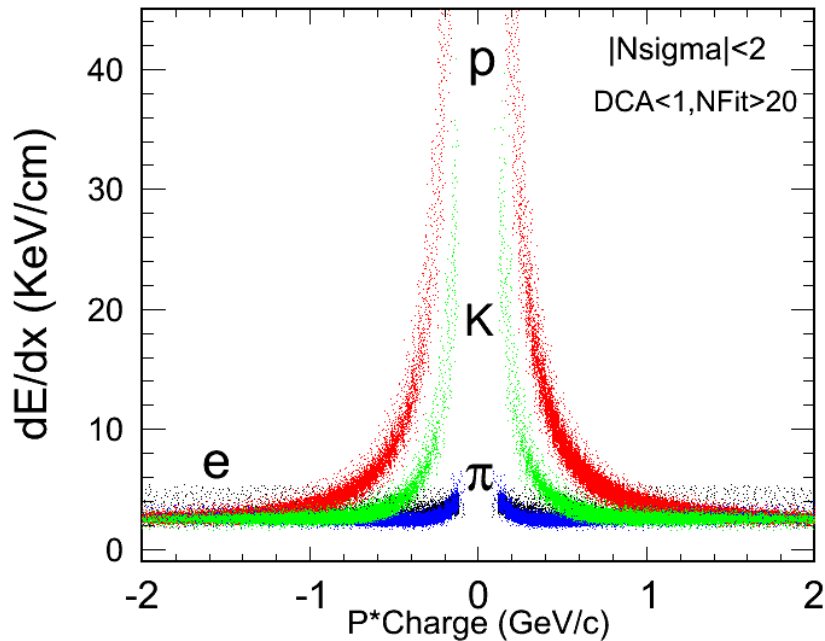
- Multiplicity dependence can be taken out and results plotted as a function of  $N_{part}$
- Possible observables:
  - Kurtosis x Variance
  - Skewness x St. Deviation
- Ratio of Susceptibilities, Volume drops out:
  - $K^* \sigma^2 \sim X^4 / X^2$
  - $S^* \sigma \sim X^3 / X^2$



## Collision centrality

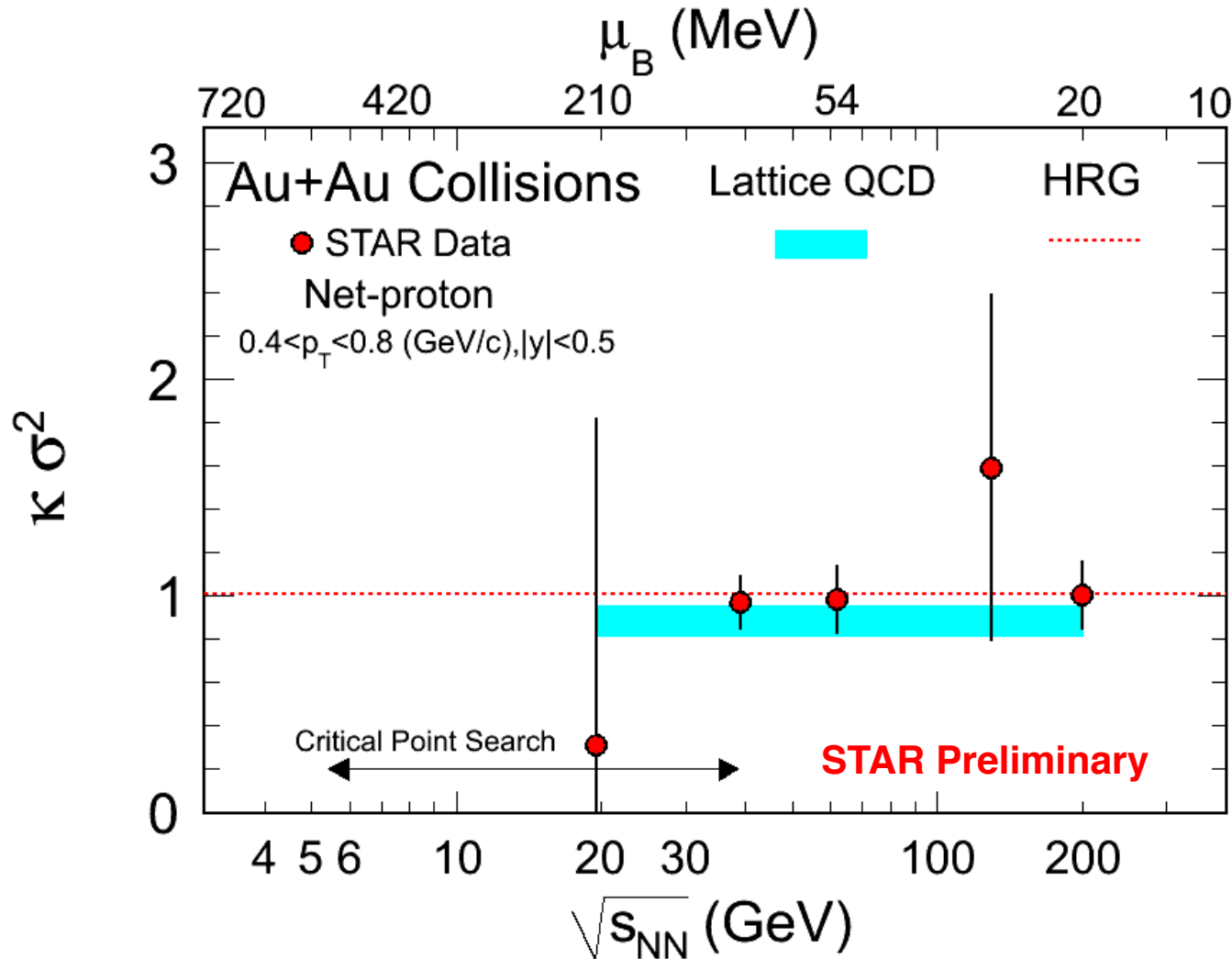
## Beam energy



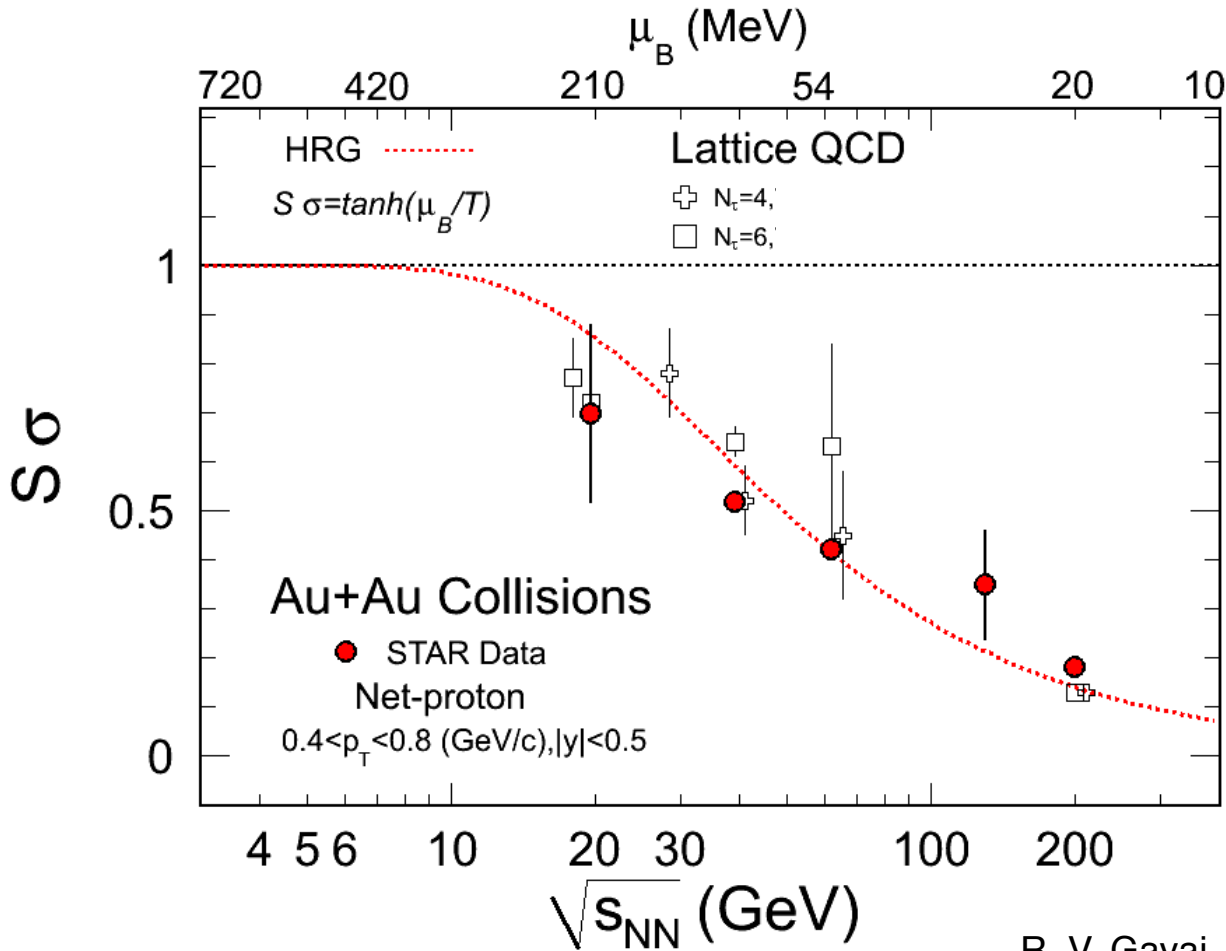


Clean Proton and anti-proton identification: TPC  $dE/dx$  with cut:

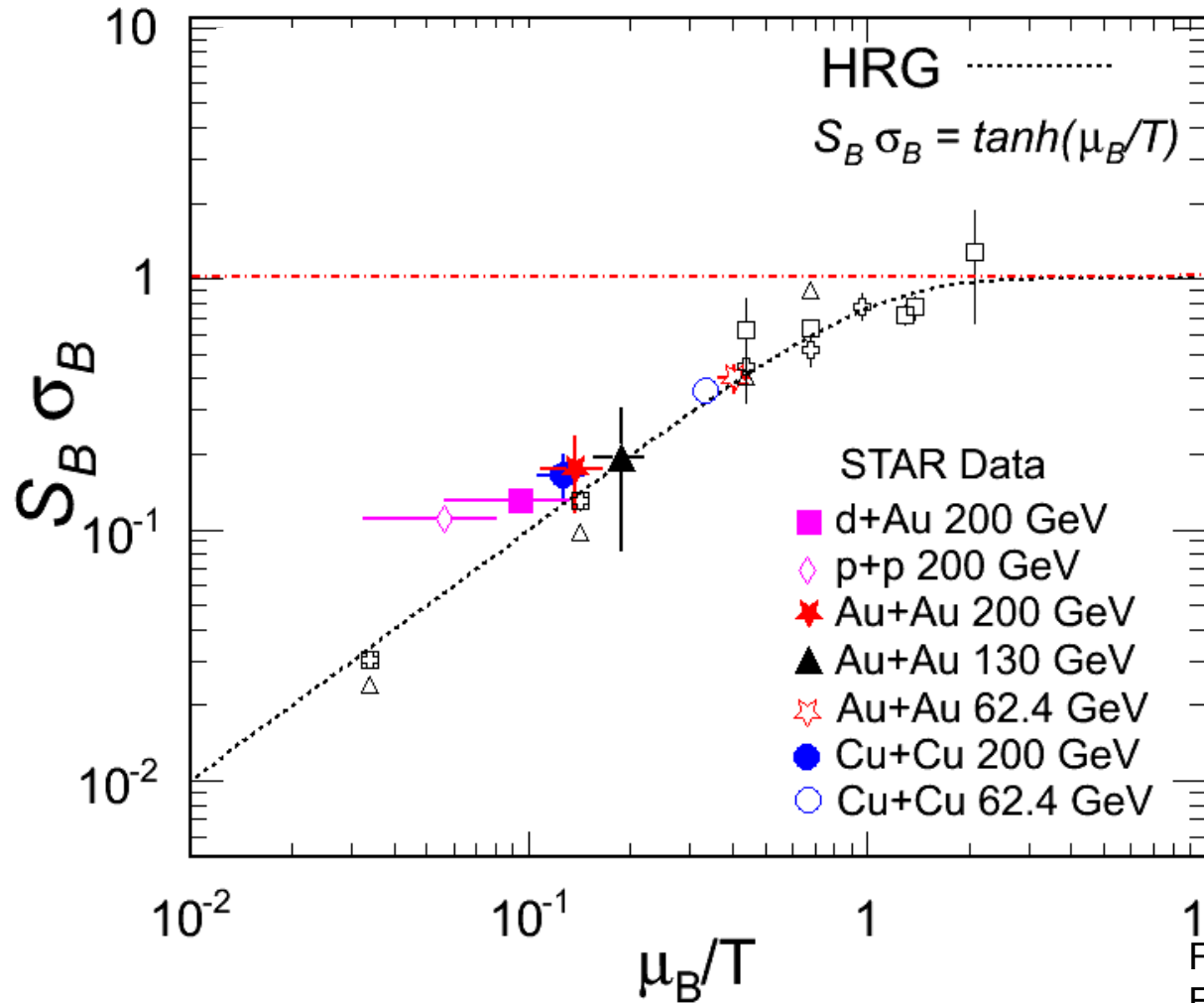
$|N_{sigmaProton}| < 2$   
 $0.4 < p_T < 0.8$  (GeV/c),  $|y| < 0.5$



For the first  
 time:  
Direct  
connection  
between data  
and lattice



R. V. Gavai, S. Gupta, arXiv: 1001.3796  
 F. Karsch, K. Redlich, arXiv: 1007.2581



**$S^* \sigma$  predicted by Lattice QCD**

R. V. Gavai, S. Gupta, arXiv: 1001.3796  
 F. Karsch, K. Redlich, arXiv: 1007.2581



# Summary



- Kurtosis and Skewness appear to be promising observables
- Relation to LQCD shown for the first time
- We are establishing the baseline (null-effect) down to  $s^{1/2} = 39 \text{ GeV}$
- STAR with its large acceptance is ideally suited for such studies